

Study of the Fastest Rate of Freezing Saline Solution Using Factorial Design Method

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Abstract An engineer needed the ability to design an experiment research to be effective and efficient to obtain optimal results. The purpose of this experiment is to determine the fastest rate of freezing saline solution. The research process begins with determining the independent variables as much as possible and determines the three independent variables to be tested. After determine variables, and then create table factorial design to determine the research steps as much as 8 times. Then determine the most influential variables using Yates's algorithm was then tested again using response surface methodology (RSM), but for this study only uses two steps of the three step RSM. So it can be concluded that the lower temperature and salinity the faster the rate of freezing for both type of salt, Krosok and salt.

Keywords Rate of Freezing, Saline Solution, Factorial Design

1. Introduction

An engineer needed the ability to design an experiment research to be effective and efficient to obtain optimal result. These experiments use factorial design methods to make it easier for researchers to get effective and efficient results.

Factorial design is a method for determining the influence of several independent variables on the response. Basically an experiment is designed to determine one variable in one response. Therefore, factorial design can make it easier to experiment with more than one

independent variable. Another use of factorial design is that it can reduce the number of experiments we have to do by studying several factors simultaneously.

The purpose of this experiment is to determine the fastest rate of freezing saline solution. The output to be produce of this study is a graph and the most influential variable as a result. In this study the output will be obtained by using factorial design and least square and response surface methodology.

2. Literature Study

2.1. Factorial Design

Factorial design is an important method to determine the effects of multiple variables on a response/output. Traditionally, experiments are designed to determine the effect of one variable upon one response/output.

There are advantages by combining the study of multiple variables in the same factorial experiment. Factorial design can reduce the number of experiments one has to perform by studying multiple factors simultaneously. Additionally, it can be used to find both main effects (from each independent factor) and interaction effects (when both factors must be used to explain the outcome).

Factorial design is a useful method to design experiments in both laboratory and industrial settings. Because factorial design can lead to a large number of trials, which can become expensive and time-consuming, factorial design is best used for a small number of variables with few states (1 to 3).

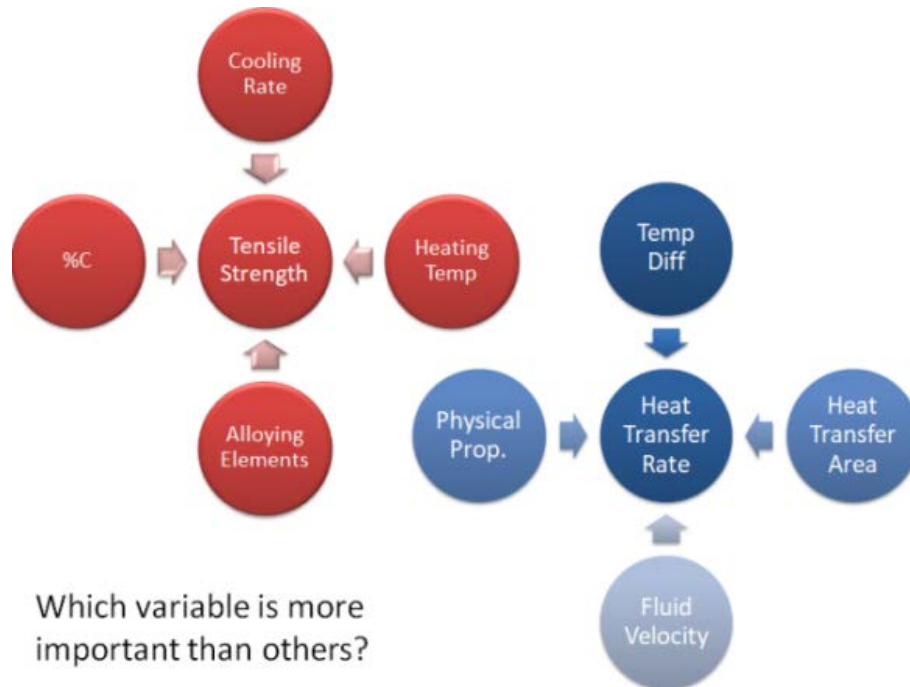


Figure 1. Important Variable

2.2. Least Square

The method of least squares is a standard approach to the approximate solution of over determined systems, i.e., sets of equations in which there are more equations than unknowns.

Least square means that the overall solution minimizes the sum of the squares of the errors made in the results of every single equation. The most important application is in data fitting.

In this equation the β 's are unknown constants to be estimated and the x have known values. One common example is where x_1, x_2, \dots are the levels of k factors, say temperature x_1 , line speed x_2 , concentration x_3 , and so on, and y is a measured response such as yield.

$$y = \beta_0 x_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_k x_k + e$$

Table 1 shows a small illustrative set of data from an experiment to determine how the initial rate of formation of an undesirable impurity y depended on two factors: **A) the concentration x_0 of monomer** and **B) the concentration of**

dimer x_1 . The mean rate of formation y was zero when both components x_0 and x_1 were zero. Over the relevant ranges of x_0 and x_1 the relationship was expected to be approximated by

$$y = \beta_0 x_0 + \beta_1 x_1 + e$$

For any particular set of trial values of the parameters β_0 and β_1 could calculate $S(\beta)$. For example, for data of Table 1, if $\beta_0 = 1$ and $\beta_1 = 7$, would get:

$$S(1,7) = \sum (y - 1x_0 - 7x_1)^2 = 1.9022$$

Thus in principle could obtain the minimum value of S by repeated calculation for a grid of trial values. It would eventually be able to construct Figure 2, a 3D plot of the sum of squares surface of $S(\beta)$ versus β_0 and β_1 . The coordinates of the minimum value of this surface are the desired least square estimates

$$b_0 = 1.21 \quad \text{and} \quad b_1 = 7.12$$

$$y = 1.21 x_0 + 7.21 x_1$$

Table 1. Initial Rate of Impurity Investigation

Observed Run Number	Order in Which Experiments Were Performed	Concentration of Monomer, x_0	Concentration of Dimmer, x_1	Initial Rate of Formation of Impurity y
1	3	0.34	0.73	5.75
2	6	0.34	0.73	4.79
3	1	0.58	0.69	5.44
4	4	1.26	0.97	9.09
5	2	1.26	0.97	8.59
6	5	1.82	0.46	5.09

Quantities needed in subsequent calculations: $\sum x_0^2 = 7.0552$, $\sum x_1^2 = 3.6353$,
 $\sum x_0 x_1 = 4.1782$, $\sum x_0 y = 38.2794$, $\sum x_1 y = 30.9388$, $\sum y^2 = 267.9245$

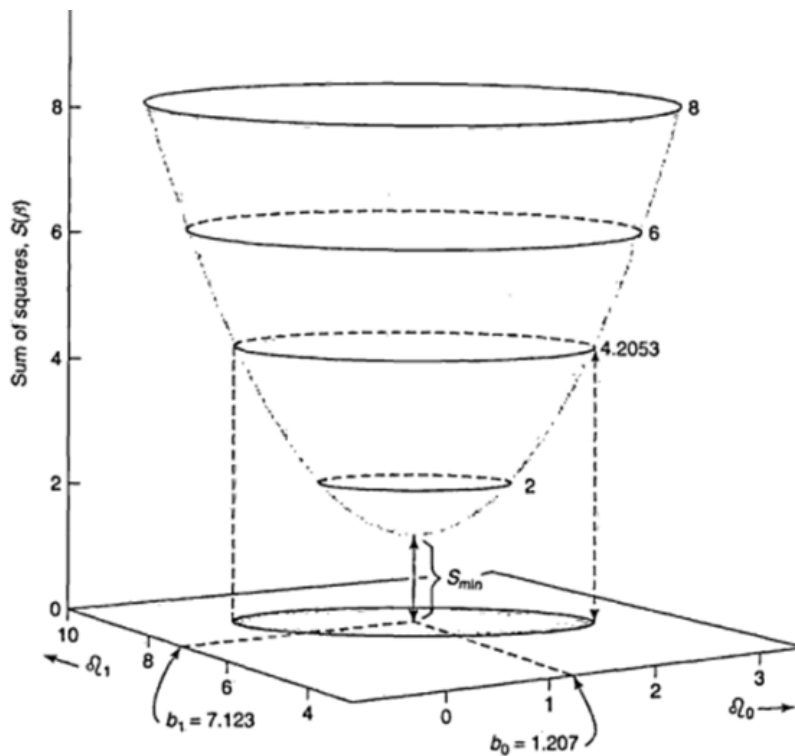


Figure 2. Sum of Square Surface: $S(\beta) = \sum (y - \beta_0 x_0 - \beta_1 x_1)^2$

2.3. Normal Equation

$$\frac{\partial S(\beta)}{\partial \beta_0} = -2(\sum y - \beta_0 \sum x_0 - \beta_1 \sum x_1) x_0 = 0$$

$$\frac{\partial S(\beta)}{\partial \beta_1} = -2(\sum y - \beta_0 \sum x_0 - \beta_1 \sum x_1) x_1 = 0$$

After simplification these become what are called the normal equations

$$b_0 \sum x_0^2 + b_1 \sum x_0 x_1 = \sum y x_0$$

$$b_0 \sum x_0 x_1 + b_1 \sum x_1^2 = \sum y x_1$$

3. Research Methodology

1) Determined Independent Variable

The independent variables determined for the design of this experiment are as follows:

- a) Freezer Temperature
- b) Refrigerator
- c) Salinity
- d) Frozen water mass
- e) Freezing time
- f) Initial water temperature
- g) Type of water
- h) Type of salt

2) After determining the independent variable for the experiment, the next step is to determine the three independent variables to be tested, while the other independent variables are fixed.

a) The independent variables to be tested are:

- Freezer Temperature (Freezer Temperature Setting)
- Freezer temperature settings are varied in:
 - Setting 4, with a temperature of -17°C
 - Setting 6, with a temperature of -19°C

- Salinity

Salinity is varied in:

- 10% salt
- 20% salt

- Type of Salt

Type of salt is varied in:

- Salt

➤ Krosok

b) Fixed free variables are:

- Refrigerator Brand
Toshiba
- Frozen Water Mass
250 grams
- Freezing Time
5 hours
- Initial Water Temperature
25°C
- Type of Water
Tap water

3) Factorial Design Method

This experiment used the 2^3 factorial design methods with two quantitative factors, temperature and salinity and one qualitative factor, the type of salt.

Table 2. Factorial Design 2^3

	Freezer Temperature	Salinity (%)	Type of Salt
+	6 (-19°C)	20	krosok
-	4 (-17°C)	10	salt

Table 3. Factorial Design

Run	Freezer Temperature (°C)	Salinity (%)	Type of Salt	Ice Mass (g)	Freezing rate (g/jam)
1	-19	20	krosok		
2	-17	20	krosok		
3	-19	10	krosok		
4	-17	10	krosok		
5	-19	20	salt		
6	-17	20	salt		
7	-19	10	Salt		
8	-17	10	Salt		

4. Results and Discussion

1) The experiment was carried out in 8x according to the design factorial table that was made before.

Table 4. Experiment Result

Freezer Temperature (°C)	Salinity (%)	Type of Salt	Ice Mass (g)	Freezing Rate (g/jam)
-19	20	Krosok	30	6
-17	20	Krosok	0	0
-19	10	Krosok	210	42
-17	10	Krosok	150	30
-19	20	Salt	0	0
-17	20	Salt	0	0
-19	10	salt	160	32
-17	10	salt	170	34

2) The Most Influential Variables

The next step after getting the results from the experiment is to determine the most influential variables. Determine the most influential variable using the Yates Algorithm method.

Table 5. Yates Algorithm

Freezing Rate (g/jam)	Yates Algorithm					
	1	2	3	divider		explanation
6	6	78	144	8	18	average
0	72	66	-16	4	-4	Freezer Temperature
42	0	-18	132	4	33	Salinity
30	66	2	-4	4	-1	Setting & Salinity
0	-6	66	-12	4	-3	Salinity
0	-12	66	20	4	5	Type & Temperature
32	0	-6	0	4	0	Type & Salinity
34	2	2	8	4	2	Type, Temperature & Salinity

Yates algorithms table above shows that the most influential variable is the salinity.

3) Result of Least Square Method

Table 6. Least Square

Freezer Temperature (°C)	Salinity (%)	Freezing Rate (gr/jam)					
T	S	FR	T ²	T.S	FR.T	S ²	FR.S
-19	20	6	361	-380	-114	400	120
-17	20	0	289	-340	0	400	0
-19	10	42	361	-190	-798	100	420
-17	10	30	289	-170	-510	100	300
-19	20	0	361	-380	0	400	0
-17	20	0	289	-340	0	400	0
-19	10	32	361	-190	-608	100	320
-17	10	34	289	-170	-578	100	340
Σ			2600	-2160	-2608	2000	1500

Normal Equation:

$$b_0 \sum T^2 + b_1 \sum TS = FRT$$

$$b_0 \sum TS + b_1 \sum S^2 = FRS$$

From the least square table, the normal equation becomes:

$$2600 b_0 - 2160 b_1 = -2608$$

$$-2160 b_0 + 2000 b_1 = 1500$$

To find the value of b0 and b1 use the Matrix, so that it is obtained:

$$b_0 = -3.6976$$

$$b_1 = -3.24341$$

So the equation obtained is:

$$FR = -3.697 T - 3.243 S$$

4) Response Surface Methodology (RSM)

a) Krosok

The first step is to use the initial first order method. This step takes 7 times experiments.

Table 7. Krosok Initial First Order Results

No	Salinity (%)	Temperature (C)	Ice Mass (gram)	Freezing Rate (g/hour)
1	20	-19	30	6
2	20	-17	0	0
3	10	-19	210	42
4	10	-17	150	30
5	15	-18	80	16
6	15	-18	90	18
7	15	-18	90	18

Determination of angles used using calculations:

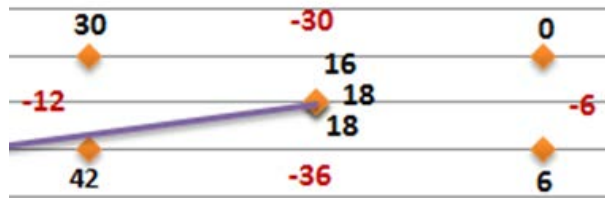


Figure 3. Krosok Angle

$$\Delta X = \frac{-36 + (-30)}{2} = -33$$

$$\Delta Y = \frac{-12 + (-6)}{2} = -9$$

$$\alpha = \text{tg} \frac{\Delta Y}{\Delta X}$$

$$= \text{tg} \frac{-9}{-33} = 15.255$$

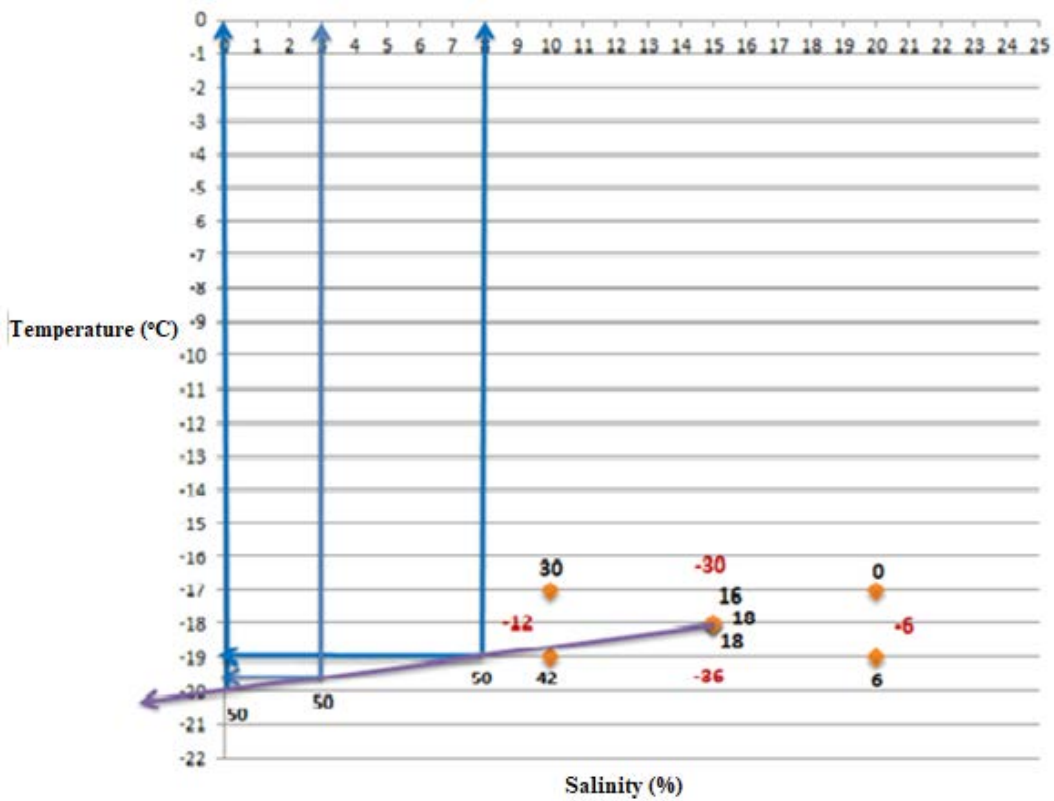


Figure 4. Graph of Experimental Results in Krosok

b) Salt

The step of this type of salt is same with Krosok. The first step is to use the initial first order method. This step takes 7 times experiments.

Table 8. Salt Initial First Order Result

No	Salinity (%)	Temperature (C)	Ice Mass (gram)	Freezing Rate (g/hour)
1	20	-19	0	0
2	20	-17	0	0
3	10	-19	160	32
4	10	-17	170	34
5	15	-18	100	20
6	15	-18	110	22
7	15	-18	100	20

Determination of angels used using calculation:

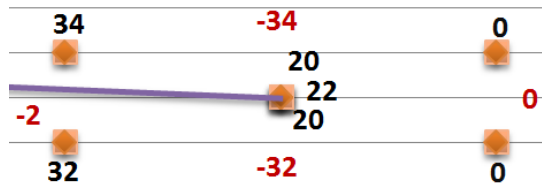


Figure 5. Salt Angle

$$\Delta X = \frac{-32 + (-34)}{2} = -33$$

$$\Delta Y = \frac{-2 + 0}{2} = -1$$

$$\alpha = \text{tg} \frac{\Delta Y}{\Delta X}$$

$$= \text{tg} \frac{-1}{-33} = 1.74$$

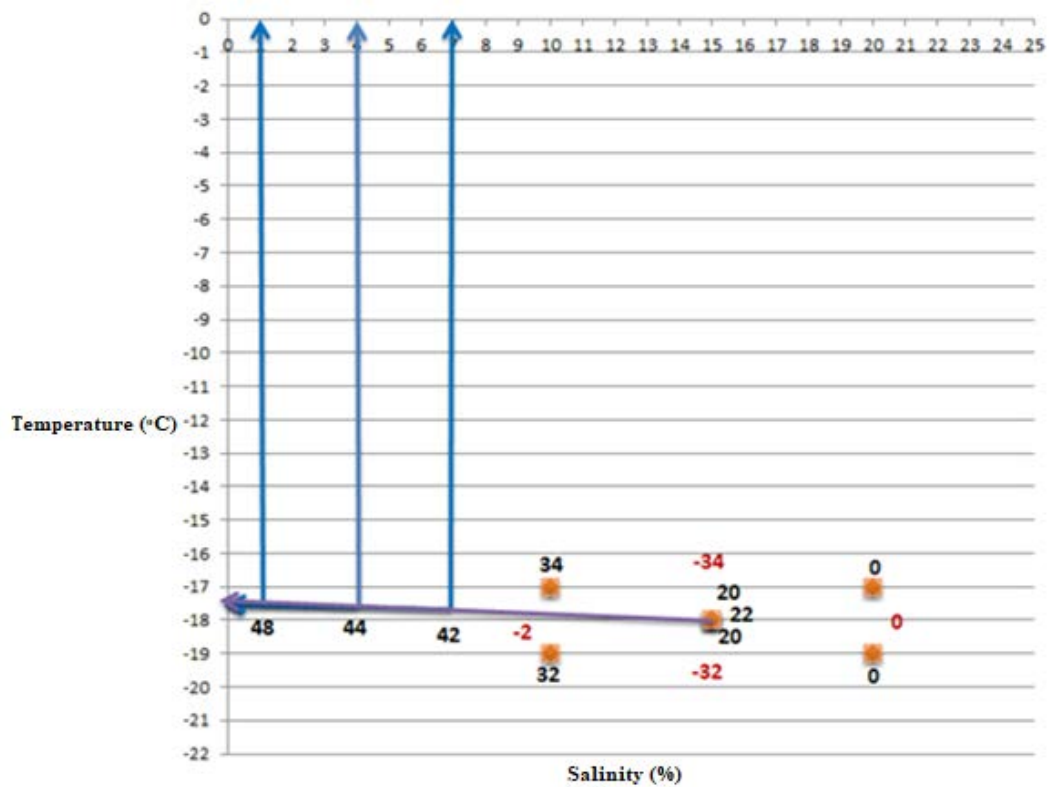


Figure 6. Graph of Experimental Results in Salt

5. Conclusions

In both types of salt cannot carry out RSM experiments for the first order secondary steps. This is caused by the following [3, 4, 5]:

- a. The results show that the value continues to decrease with a maximum freezing rate of 50 g/hour and constant for Krosok and 48 g/hour and continues to decrease to 50 g/hour constant for salt.
- b. Change in the percentage of salinity is limited because if the water adds more salt, it will become saturated so that it cannot dissolve completely.
- c. The freezer temperature changes are limited according to the specifications of the refrigerator.

On the graph of the Krosok, the freezing rate tends to the bottom left at an angle of 15.25° . On the graph of the salt, the freezing rate tends to the upper left with an angle of 1.74° . This indicates that the salinity is more influential than the temperature of the freezer.

The results obtained for both types of salt are, the lower the salt content, the faster the freezing rate. As for the type of salt, the fastest freezing rate according to the results of the data obtained is salt.

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