

New and Renewed Variations on Prime Numbers

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Abstract In this article the why and how of the prime numbers were shown; to be more specific, I present the pattern that is defined, i.e. every prime number is in the interval between $(30a + (p))$ and $(42a + (p_1))$; $p = (11;17;23;29)$; $p_1 = (13; 19; 25; 31; 37; 43)$. This verifies the accuracy of the series of Dirichelet, and improvement, because any series that of a prime number matches the prime number of this pattern. Another contribution of this work is to know whether a number is prime; both for a small number, as for one he is infinitely large, without applying the process of factorization.

Keywords Arithmetic, Group $(G_5; G_7)$, Equation Twin Prime Number

Mathematic Subject Classification 11Axx

1 Introduction

If by definition a prime number is any entire number whose only divisors are unit and himself.

$$p \in (2c + 1)$$

$$\exists p \in (2c)$$

[1]We know that the process for have odd numbers in sum is $(1 + 2 + 2 + 2 + \dots)$, consequently this is the same thing that $(3 + 2 + 2 + 2 + \dots)$ is to say $(3 + 2n)$. Of general form we will say $(x + xn = 2c + 1)$. The prime numbers are necessary to cover the gaps left by correlative multiplication. If we multiply $3(2c + 1)$ we have the larger spaces without numbers; at multiply by the rest of the odd numbers it is obvious that the free spaces are reduced. The next number is $5 = (3 + 2)$.

In $(3 + 2)(2c + 1)$ we will have the same values that we have with the number three, more $2(2c + 1)$, the value $2(2c + 1)$ fills the gaps of the number three. This is true for each and every one the products greater than three. For certain values of $[2(2c + 1) = 6n]$ we note that this value matches in the space of a product of the number three; always that $(2c + 1) = 3n$.

This synthesis shows that the primes will have a pattern that generates primes, with a difference maxim between them (consecutive) of six units.

It also verifies that:

$$\forall [(30a + (p)); (42a + (p_1))] = 2c + 1$$

because: $(p) - 1 = 2n$.

but not:

$$\forall 2c + 1 = ([30a + (p)]; [42a + (p_1)])$$

as shown by the following equation:

$$\frac{\exists(2c + 1) - (5; 7)}{6} \neq Z$$

2 Main results

In next step is define the interval of primes and, the because its roots are not all prime. I begin with the series Dirichelet[2] whose numerical values are closest to zero.

$$3 + 6a; 5 + 6a; 7 + 6a$$

The expression $(3 + 6a)$ is discarded because it is always $3(2c + 1)$. The other two with a values of $(a \neq 5n; 7n)$ they can not have factor and therefore we can have primes. However when we give values to (a) one of they will be a multiple of $(5n; 7n)$ to avoid this multiple, we situate in (a) the following. $[5a + (1; 2; 3; 4)]$ and $[7a + (1; 2; 3; 4; 5; 6)]$ and we have.[1][2]

$$G_5 \rightarrow 5 + 6[5a + (1; 2; 3; 4)] = p$$

$$G_7 \rightarrow 7 + 6[7a + (1; 2; 3; 4; 5; 6)] = p$$

it is true that we have avoided the factor $(5n; 7n)$ and therefore a priori could say that all its roots are prime numbers. In its development I verified that it is not, because when (a) has the value of a product of the addends (p) or (p_1) , the equations they have by integer root and is not a prime.

$$5 + 6[5a + (1; 2; 3; 4)] = 30a + (11; 17; 23; 29)$$

$$7 + 6[7a + (1; 2; 3; 4; 5; 6)] = 42a + (13; 19; 25; 31; 37; 43)$$

By the equations following we can know when (a) is one sum of the product (p) or (p_1) .

$$\frac{5 + 6[5a + (1; 2; 3; 4)]}{(11; 17; 23; 29)} = Z$$

$$\frac{7 + 6[7a + (1; 2; 3; 4; 5; 6)]}{(13; 19; 25; 31; 37; 43)} = Z$$

To determine if an odd number is prime or not, the first one, has to belong the group $(G_5; G_7)$.

If the roots is not an integer, then it will be a prime number, if not, it will be a product of prime number between group five and seven or among the same group in all possible combinations. Are large but finite.

In all them are true that:

$$\forall [30a + (p)] \times [42a + (p_1)] = [42b + (p_1); 30a + (p)]$$

$$[30a + p] \times [30a + (p)] =$$

$$[42a + p_1] \times [42a + (p_1)] =$$

$$[3a + (p)]^n =$$

.....

In all these equations there is an addend that is the product of primes (p) or (p_1)

By example: $[30a + (p)] \times [42a + (p_1)]$

(i)

$$30a \times 42a + 30a \times (p_1) + (p) \times 42a + (p) \times (p_1) = [42b + (p_1)]; [30b + (p)]$$

$$30a \times 42a + 30a \times (p) + (p_1) \times 42a + (p) \times (p_1) - [(p); (p_1)] = (42b; 30b)$$

By the addend $(p \times p_1)$ is corroborate the why in all product of the group (G_5) and (G_7) we have the root of a group (G_5) or (G_7) . As we see now.

$$[(p) \times (p_1)] - ((p); (p_1)) = 3n$$

It is the only value that allows the exact division; therefore we dividing by three in (i) we have.

$10a \times 14a + 10a \times (p_1) + (p) \times 14a + n = 14b; 10b$; (n) it is always a even number, therefore is simplified in the shape.

$$5a \times 7a + 5a \times (p_1) + (p) \times 7a + n' = (5b; 7b)$$

If we substitute the value of $(5b; 7b)$ in $(5a; 7a)$ of the equations $5 + 6[5a + (1; 2; 3; 4)]$; $7 + 6[7a + (1; 2; 3; 4; 5; 6)]$.

We have a number that is origin of they and is not prime, so it is a product of two primes, however we have more options in $(G_5; G_7)$ for define primes numbers; simply changing in the root the value of $(p; p_1)$. We know the existence of nine different roots for each (a) . The same is applies to each of the products and power.

Also the fundamental theorem of arithmetic it is corrobora, because if will exist a number in $(G_5 \text{ or } G_7)$ that will not be prime or product of primes, then the theorem will be false.

proof.2

Axiom: $\forall((p) \times (p_1)) - [(p); (p_1)] = 3n; 5n; 7m; \text{ with } (n = 2n)$
and therefore:

$$(p) \times (p_1) \notin [5 + 6[5a + (1; 2; 3; 4)]; 7 + 6[7a + (1; 2; 3; 4; 5; 6)]]$$

and so is verified for being:

$$(p) \times (p_1) = [30a + (p); 42a + (p_1)] - [42a \times (p_1) + 30a \times (p) + 42a \times 30a]$$

With the axiom, we say that:

$$\frac{[(p) \times (p_1)]^n - ((p); (p_1))}{3} = m$$

This implies an equality with the product, ie.

$$\frac{[(p) \times (p_1)]^n - ((p); (p_1))}{m} = \frac{[(p) \times (p_1)] - ((p); (p_1))}{n'}$$

If we subtract in they the value of three we have.

$$\frac{[(p) \times (p_1)]^n - ((p); (p_1))}{m} - 3 = \frac{[(p) \times (p_1)] - ((p); (p_1))}{n'} - 3 = 0$$

and therefore:

$$[(p) \times (p_1)]^n - ((p); (p_1)) - 3m = [(p) \times (p_1)] - ((p); (p_1)) - 3n' = 0$$

As admits in $((p); (p_1))$, the same value in the two terms we have:

$$[(p) \times (p_1)]^n - 3m = [(p) \times (p_1)] - 3n'$$

$$\frac{[(p) \times (p_1)]^n - [(p) \times (p_1)]}{3} = m - n$$

Whereby:

$$\forall \frac{(G_5 \times G_7)^n - [(p) \times (p_1)]}{3} = m - n'$$

This allows know when (N) is one power or a product of primes **Transcendent for the problem (P = NP)[3]**.
And also is verifying that.

$$\exists(2c + 1) \notin [G_5; G_7]$$

as they are:

$$(3n; 5n; 7n; [5 + 6a; a < 5]; [7 + 6a; a < 7]; (p) \times (p_1); p \times (p_1); (p) \times (p); p_1 \times (p_1))$$

3 Conclusion

Every number ($Z_p > 7$) has its origin in the group $[G_5; G_7]$ and is in the interval between.

$$[30a + (p)] \text{ and } [42a + (p_1)]$$

If this were not so, I would be inside.

$$(2c + 1) \notin [G_5; G_7]$$

and no are prime.

Step to shown, as go from group five through seven, or vice versa.

$$G_5 \rightarrow G_7 = \frac{(30a + 29) + |2[6a - 8] - \sum 2|_{lm=2}}{(3; 5; 7)} \neq Z = Z_p \in (G_5; G_7)$$

$$G_7 \rightarrow G_5 = \frac{(42a + 43) - |2[6a + 1] - \sum 2|_{lm=2}}{(3; 5; 7)} \neq Z = Z_p \in (G_5; G_7)$$

4 Discussion

First

To verify if a number (N= odd) is prime, must meet the following equations.

$$\sqrt{N}$$

$$\frac{N}{(3; 5; 7; 11; 17; 23; 29)} \neq Z$$

$$\frac{N}{13; 19; 25; 31; 37; 43)} \neq Z$$

$$\frac{N - (p \times (p))}{(30; 42)} \neq Z$$

$$\frac{N - (p_1 \times (p_1))}{(30; 42)} \neq Z$$

$$\frac{N - (p) \times (p_1)}{(30; 42)} \neq Z$$

$$\frac{N - (p) \times (p_1)}{3} \neq Z$$

The latter equation can replace the previous three.

And, for differentiate the powers and producted between primes of a prime number, also we have the following..

$$\frac{N - 5}{6} = Z \rightarrow [Z = 5a + (1; 2; 3; 4)]$$

Or

$$\frac{N - 7}{6} = Z \rightarrow [Z = 7a + (1; 2; 3; 4; 5; 6)]$$

Depending on which is his origin, is started the process, ie with the five or seven.

$$\frac{Z - (1; 2; 3; 4)}{5} = z; \frac{z - (1; 2; 3; 4)}{6} = z_1; \frac{z_1 - (1; 2; 3; 4)}{5} \neq z$$

When you reach a root not exact, we pass this value (z) to:

$$\frac{z - (1; 2; 3; 4; 5; 6)}{7} = z; \frac{z - (1; 2; 3; 4; 5; 6)}{7} = z; \frac{z - (1; 2; 3; 4; 5; 6)}{7} \neq z$$

If (N) meets all the above steps; (N) is a prime number.

Second

The last step in the development of prime number is for generate only, twin primes.

It is obvious that these are already included in ($G_5; G_7$) and therefore, begin has to be met the following.

$$5a + (1; 2; 3; 4) = 7a + (1; 2; 3; 4; 5; 6)$$

Or from equation following.

$$7 + 6[7a + (1; 2; 3; 4; 5; 6)] - 2 = 5 + 6[7a + (1; 2; 3; 4; 5; 6)]$$

with this equation we know, the minor of the primes, by being.

$$\forall(5 + 6[7a + (1; 2; 3; 4; 5; 6)]) = 5 + 6[5a + (1; 2; 3; 4)]$$

with ($a \neq a; a > 1$) if is not met, not there are twin primes.

and if it is met, have of verify with equation following.

$$\frac{5 + 6[7a + (1; 2; 3; 4; 5; 6)]}{(5; 11; 17; 23; 29; 41)} \neq Z = p$$

and therefore the following prime number is define with the equation following.

$$\frac{(p+2)}{5} \neq Z = p_n$$

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