Sensitivity and Uncertainty Analysis of the Keff Due to ENDF/B-VII.0 Cross Sections Uncertainties of the Major Isotopes in Nuclear Reactors

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Abstract The main objective of this study is to estimate nuclear data uncertainties on the effective multiplication factor (Keff) related to elastic, inelastic, capture and fission cross sections and the correlations between them. Different rapid and thermal cases of the different IHECSBE benchmarks have been studied by using nuclear data evaluation ENDF/B-VII.0 to calculate the sensitivity vectors for ¹H, ¹⁶O, ²³⁵U and ²³⁸U isotopes and four cases used to validate our sensitivity vectors. These sensitivity vectors are calculated by using the adjoint-weighted perturbation method based on the Kpert card of the Monte Carlo code MCNP6. Thus, the uncertainties induced by nuclear data have been calculated by combining the sensitivity vectors with the covariance matrices that are generated by the ERRORJ module of the recently updated of the nuclear data processing system NJOY99. In this study, we found several cross sections and covariance matrices lack the adjustment: the four cross sections (elastic, inelastic, capture and fission) of the ²³⁵U and their covariance matrices Lack the adjustment especially in the rapid energies; the elastic cross section of the ¹⁶O, the elastic and capture cross sections of the ¹H and their covariance matrices lack the adjustment especially in the thermal energies.

Keywords Cross Section, Sensitivity, Covariance Matrix, Nuclear Uncertainty, MCNP6

1. Introduction

Since the beginning of the century, the nuclear data evaluation communities are putting more and more attention to the assessment of uncertainties. This increased interest concerns both basic data (cross section, emission spectrum ...) and calculated quantities for large systems. Such as neutron multiplication factor Keff, reactivity,

reaction rate and others.

With the large availability of the covariance files, as in the ENDF/B-VII.0 [1] nuclear data evaluation, more and more studies are started using this information to deduce target accuracies for neutronic parameters in future reactors and therefore future priorities for experimental measurements of differential data.

Several probabilistic and deterministic codes are made for the analysis of the sensitivity and the uncertainties of the nuclear data on the integral nuclear parameters (SCALE, MCNP, KENO, DRAGON...). Most of these codes used the multigroup adjoint-weighted technique. Except MCNP6 [2] computed the changes in a tally response (such as Keff-eigenvalue) by using the differential operator technique with continuous energy spectrum [3]. Now, it compute the changes in reactivity strictly in Keff-eigenvalue problems by using the adjoint-weighted methodology with continuous energy spectrum [4,5]. The technique of differential operator considered the source of neutrons unperturbed [6]. The sensitivity with continuous energy spectrum has no problem of the self shielding effect than the sensitivity with multigroup energy spectrum [7,8]. For this, we used the adjoint-weighted technique with continuous energy spectrum to calculate the sensitivity profiles in this work. The sensitivity profiles and covariance matrices are combined in order to obtain final uncertainties [9].

Several sensitivities and uncertainties analysis for improving and adjusting the cross sections of the important isotopes in nuclear data evaluation ENDF/B-VII.0 and in simple and complex nuclear systems are done by different codes and different perturbation techniques [10, 11]. But, there are still errors on the integral nuclear parameters due to cross sections uncertainties of the ²³⁵U, ¹⁶O and ¹H in ENDF/B.VII.0. These errors are detected with the new adjoint-weighted technique of the MCNP6 code.

In this work, a sensitivity and uncertainty analysis have

been performed for certain cases of the different IHECSBE (International Handbook of Evaluated Criticality Safety Benchmark Experiments) [12] benchmarks by using the MCNP6 and NJOY99 [13] codes. Results of the uncertainty calculated by the adjoint-weighted theory and produced by elastic, inelastic, capture and fission nuclear data on the multiplication factor are presented and analyzed.

2. Methodology and Study Approach

2.1. Adjoint-weighted Technique

Starting from the nuclear transport equation and applying a first-order perturbation, the following expression for the change in reactivity ρ can be derived [4]:

$$\Delta\rho = -\frac{\langle\psi^+, P\psi\rangle}{\langle\psi^+, F'\psi\rangle} \quad (1)$$

The reactivity is related to K_{eff} in the typical way:

$$\rho = \frac{(K_{eff}-1)}{K_{eff}} \quad (2)$$

The angular flux in the unperturbed system is ψ and its adjoint is denoted by ψ^+ . P is the operator for the perturbation taking the form:

$$P = \Delta\Sigma_t - \Delta S - \lambda\Delta F \quad (3)$$

The eigenvalue λ is:

$$\lambda = \frac{1}{K_{eff}} \quad (4)$$

And the three terms in P from left to right, are the change in the total cross section, the change in scattering operator, and the change in the fission multiplication operator. F' is the perturbed fission operator.

Monte Carlo technique can be used to sample the numerator and the denominator in continuous-energy forward calculation [4] and the change in reactivity can be estimated by taking the ratio in (1).

We express change in cross section as:

$$\Delta\sigma_x = f\sigma_x \quad (5)$$

We apply the relationship:

$$\Delta K_{eff} = K_{eff} \frac{K_{eff}\Delta\rho}{1-K_{eff}\Delta\rho} \quad (6)$$

We compute sensitivity coefficients by:

$$S_{K_{eff},\sigma_x} \approx \frac{1}{f} \frac{K_{eff}\Delta\rho}{1-K_{eff}\Delta\rho} \quad (7)$$

The quantity $K_{eff}\Delta\rho$ scales linearly with f ; can make arbitrarily small until sensitivity becomes sufficiently precise.

2.2. Study Approach

During this study:

We have selected a different criticality safety cases of IHECSBE [12] benchmarks.

We have studied the impact of the cross sections uncertainties for ^1H , ^{16}O , ^{235}U , and ^{238}U isotopes on the effective multiplication factor uncertainty in each selected case. The selected isotopes are generally known by their important contribution in the effective multiplication factor calculation.

The sensitivity vectors for multiplication factor were generated by using Kpert card of MCNP6 code in 15 energy groups, they are represented in table 1.

Table 1. Fifteen energy groups used in our sensitivity and uncertainty analysis

Groups numbers	Energy groups (Mev)
1	0.00E 00 - 1.10E-07
2	1.10E-07 - 5.40E-07
3	5.40E-07 - 4.00E-06
4	4.00E-06 - 2.26E-05
5	2.26E-05 - 4.54E-04
6	4.54E-04 - 2.04E-03
7	2.04E-03 - 9.12E-03
8	9.12E-03 - 2.48E-02
9	2.48E-02 - 6.74E-02
10	6.74E-02 - 1.83E-01
11	1.83E-01 - 4.98E-01
12	4.98E-01 - 1.35E00
13	1.35E00 - 2.23E00
14	2.23E00 - 6.07E00
15	6.07E00 - 19.60E00

The covariance matrices generated by ERRORJ module of the NJOY99 [13] processing system based on the same discretization of the sensitivity energy. The values of the covariance were computed for fifteen energy groups mentioned above by using a weighting flux that corresponds to the $1/E$ + fission spectrum + thermal maxwellian shape. For all cases, an infinite dilution condition was assumed ($\sigma_0=1 \cdot 10^{10}$ barns) and the temperature was considered to be 300K.

The steps adopted in this study are presented in Figure 1:

- The perturbation approach is generally based on the NJOY99 processing system, the MCNP6 code and the program for calculating the total uncertainty produced by nuclear data ($\Delta K_{eff-nucl}$).
- Inputs are the MCNP6 input file and ENDF/B-VII.0 file containing the matrices of covariances. As shown in figure 1, ENDF/B-VII.0 file is processed by NJOY99 in order to produce cross sections in the ACE format and covariance matrices used by program for calculating $\Delta K_{eff-nucl}$.
- The sensitivity vectors were calculated by using the most commonly used radiation transport code MCNP6. The sensitivity profiles $S_{K_{eff},\sigma_{x,g}}$ are defined as the relative

change in a response Keff (the effective multiplication factor) with respect to cross section σ_x in a particular energy group g, it is defined as:

$$S_{Keff,\sigma_x,g} = \frac{\sigma_{x,g} \Delta Keff}{Keff \Delta \sigma_{x,g}} \approx \frac{1}{f} \frac{Keff \Delta \rho}{1 - Keff \Delta \rho} \quad (8)$$

- The sensitivity profile $S_{Keff,\sigma_x,g}$ is obtained by using the perturbation option of MCNP6 that is defined in Kpert card by using the first-order perturbation by the adjoint-weighted technique.

- The cross sections were perturbed as described in the following steps:

1. Four cross sections will be considered: elastic, inelastic, capture and fission cross section, and only one specific cross section in one energy group and one isotope varied each time.

2. Then a material card is created in which the atomic density for the relevant isotope is increased by 1%.

3. The Kpert card is then created specifying that: the relevant material is replaced by the perturbed material in each of the cells in which the material is present. Perturbation cards are given for all energy groups.

4. Finally, MCNP6 is run with this modification in the input; and in the output file a table is given with the results of different perturbations and their related statistical uncertainties.

- These sensitivity vectors must be combined with covariances matrices (10) and (11), by using a program

calculating Keff uncertainties in similar energy groups.

- The total uncertainty is calculated by using the following equation [9]:

$$\frac{\Delta Keff}{Keff} = \sqrt{\sum_i \sum_{\sigma_x} \sum_g \left[\frac{\Delta Keff}{Keff} \right]_{i,\sigma_x,g}^2} \quad (9)$$

i: index of material

σ_x : index of reaction cross section

g: index of energy group

- The contribution of every nuclide-reaction in $\frac{\Delta Keff}{Keff}$ is calculated as follows [5]:

$$\left\{ \begin{array}{l} \sqrt{S_{Keff,\sigma_x,g} \text{cov}(\sigma_x,g, \sigma_y,g') S_{Keff,\sigma_y,g'}} \quad (10) \\ - \sqrt{|S_{Keff,\sigma_x,g} \text{cov}(\sigma_x,g, \sigma_y,g') S_{Keff,\sigma_y,g'}|} \quad (11) \end{array} \right.$$

If $(S_{Keff,\sigma_x,g} \text{cov}(\sigma_x,g, \sigma_y,g') S_{Keff,\sigma_y,g'}) \geq 0$, we have using the equation (10).

If $(S_{Keff,\sigma_x,g} \text{cov}(\sigma_x,g, \sigma_y,g') S_{Keff,\sigma_y,g'}) < 0$, we have using the equation (11).

$S_{Keff,\sigma_x,g}$: Sensitivity coefficient for Keff due to the neutron cross section σ_x , and energy group g.

$\text{cov}(\sigma_x,g, \sigma_y,g')$: Covariance matrix that comprises covariance data for two cross sections (σ_x, σ_y) in the energy groups g and g'.

Figure 1. Flowchart of the uncertainty calculation by MCNP6 and NJOY99 codes

3. Effective Multiplication Factors Calculated by MCNP6

The K_{eff} values with their related standard deviations for the cases studied are listed in table 2. The third column represent values from the International Criticality Safty Benchmark experements (IHECSBE). Our results calculated by MCNP6 code and ENDF/B-VII.0 nuclear data evaluation are represented in the second column.

We chose these cases because their relative differences between the experimental K_{eff} and the calculated K_{eff} are higher than their experimental uncertainties and their standard deviations.

Table 2. HEU-SOL-THERM-001-cases K_{eff} and its standard deviation

Cases of benchmarks	$K_{eff} \pm \text{std. dev.}^1$ (MCNP6)	$K_{eff} \pm \Delta K_{eff}^2$ (IHECSBE)
HEU-MET-FAST-004-001 (hmf004-001)	0.99987 ± 0.00023	0.99850 ± 0.0000
HEU-MET-FAST-008-001 (hmf008-001)	0.99615 ± 0.00019	0.99890 ± 0.0016
HEU-MET-FAST-015-001 (hmf015-001)	0.99445 ± 0.00019	0.99960 ± 0.0017
HEU-SOL-THERM-006-001 (hst006-001)	0.98229 ± 0.00031	0.99730 ± 0.0050
HEU-SOL-THERM-011-001 (hst011-001)	1.00466 ± 0.00025	1.00000 ± 0.0023
HEU-SOL-THERM-016-001 (hst016-001)	0.99022 ± 0.00036	1.00000 ± 0.0036
HEU-SOL-THERM-018-001 (hst018-001)	0.98739 ± 0.00040	1.00000 ± 0.0034
HEU-SOL-THERM-028-001 (hst028-001)	0.99640 ± 0.00031	1.00000 ± 0.0023
HEU-SOL-THERM-035-007 (hst035-007)	1.00540 ± 0.00034	1.00000 ± 0.0035
HEU-SOL-THERM-037-001 (hst037-001)	1.00934 ± 0.00010	0.99800 ± 0.0034

¹This uncertainty means the statistical uncertainty or standard deviation in MCNP6 calculated with the Monte Carlo technique.

²This uncertainty means the experimental uncertainty due to uncertainties in critical heights, uncertainties in solution constituents, and in isotropic constituents [12].

4. Validation of Sensitivity Results

The calculation of the sensitivities coefficients by the adjoint-weighted technique is new in the code MCNP6; for this, we compared the results of this technique with the results of the old technique in MCNP code (differential operator technique) and with the sensitivities coefficients which are in IHECSBE and calculated by the KENO code. Also, we compared the results of the adjoint-weighted

technique between tree nuclear data evaluations ENDFB/VI.8, ENDFB/VII.0 and JENDL-4.0 [14]. This comparison is used in 30 energy groups, they are represented in table 3.

Table 3. Thirty energy groups used in our sensitivity validation

Groups numbers	Energy groups (Mev)
1	0.00E+0 - 1.00E-02
2	1.00E-02 - 2.15E-02
3	2.15E-02 - 4.64E-02
4	4.64E-02 - 1.00E-01
5	1.00E-01 - 2.15E-01
6	2.15E-01 - 4.64E-01
7	4.64E-01 - 1.00E+00
8	1.00E+00 - 2.15E+00
9	2.15E+00 - 4.64E+00
10	4.64E+00 - 1.00E+01
11	1.00E+01 - 2.15E+01
12	2.15E+01 - 4.64E+01
13	4.64E+01 - 1.00E+02
14	1.00E+02 - 2.15E+02
15	2.15E+02 - 4.64E+02
16	4.64E+02 - 1.00E+03
17	1.00E+03 - 2.15E+03
18	2.15E+03 - 4.64E+03
19	4.64E+03 - 1.00E+04
20	1.00E+04 - 2.15E+04
21	2.15E+04 - 4.64E+04
22	4.64E+04 - 1.00E+05
23	1.00E+05 - 2.00E+05
24	2.00E+05 - 4.00E+05
25	4.00E+05 - 8.00E+05
26	8.00E+05 - 1.40E+06
27	1.40E+06 - 2.50E+06
28	2.50E+06 - 4.00E+06
29	4.00E+06 - 6.50E+06
30	6.50E+06 - 6.50E+06

The figures below show the results of the sensitivity validation in rapid experiment: Godiva (highly enriched uranium sphere), hmf004-001 and hmf018-001, and in thermal experiment hst001-001; for four reactions: elastic and inelastic scattering, capture and fission.

The differences between the results of sensitivities in the above figures (2, 3, 4, 5) are due to:

- The difference between the nuclear data evaluation used.
- The difference between the perturbation techniques used: in the differential operator technique, the fundamental eigenfuction (fission distribution) approximated as unperturbed.
- The absence of thermal neutron scattering: $S(\alpha, \beta)$ in the KENO code.
- The difference between the two codes: MCNP6 uses continuous energy, KENO uses multigroup energy.

In general, the adjoint-weighted technique has the same allure with other technique. Then, it is validated.

Figure 2. Sensitivities of ^{235}U elastic and inelastic scattering, capture and fission cross sections in Godiva

Figure 3. Sensitivities of ^{235}U elastic and inelastic scattering, capture and fission cross sections in hmf004-001

Figure 4. Sensitivities of ^{235}U elastic and inelastic scattering, capture and fission cross sections in hmf018-001

Figure 5. Sensitivities of ^{235}U elastic and inelastic scattering, capture and fission cross sections in hst001-001

Figure 6. Uncertainties (pcm) produced by different cross sections of ^{235}U for different experiences

5. Uncertainty Analysis

5.1. Uncertainty on the Keff Produced by the Nuclear Data Uncertainties of the ^{235}U

Figure 6 shows the effect of cross sections uncertainties related to ^{235}U isotope on the effective multiplication factor (nucl. uncert. on Keff or $\Delta\text{Keff-nucl.}$) in different nuclear experiences. The uncertainties on the Keff produced by elastic, inelastic scattering, capture and fission cross sections and the effect of the correlation between them are represented by adjoint-weighted technique and by pcm ($1\text{pcm} = 10^{-5}$)

5.2. Interpretations and Conclusions on the Results of ^{235}U

- The elastic, inelastic, capture and fission cross sections and the correlations between them for ^{235}U in the rapid experiences, they have large contribution of uncertainties in the effective multiplication factor uncertainties ($\Delta\text{Keff-nucl.}$). Then, these four cross sections and their covariance matrices in ^{235}U require the adjustment in the rapid energies.

- The elastic, inelastic, capture and fission cross sections uncertainties and the correlations between them for ^{235}U in the thermal experiences, they have small contribution of uncertainties in the effective multiplication factor uncertainties ($\Delta\text{Keff-nucl.}$) than its contribution of uncertainties in $\Delta\text{Keff-nucl.}$ of the rapid experiences. But, in another study we found $\Delta\text{Keff-nucl.}$ increases with small increase in the atomic density for ^{235}U in six cases of hst001 [15]. Thus, we cannot assure the accuracy of these cross sections and their covariances matrices in the thermal energies when the ^{235}U atomic density increases.

5.3. Uncertainty on the Keff Produced by the Nuclear Data Uncertainties of the ^{238}U

Figure 7 shows the effect of cross sections uncertainties related to ^{238}U isotope on the effective multiplication factor (nucl. uncert. on Keff or $\Delta\text{Keff-nucl.}$) in different nuclear experiences. The uncertainties on the Keff produced by elastic, inelastic scattering, capture and fission cross sections and the effect of the correlation between them are represented by adjoint-weighted technique and by pcm ($1\text{pcm} = 10^{-5}$).

5.4. Interpretations and Conclusions on the Results of ^{238}U

- The effect of elastic, inelastic, capture and fission cross sections uncertainties related to ^{238}U on the effective multiplication factor uncertainties is very small in the thermal experiences than the rapid experiences; and that is due to the small contribution of ^{238}U cross sections on the Keff in the thermal energies. Then, in this study, we can conclude that: these cross sections and their covariance matrices do not lack the adjustment in the thermal energies.

- In another study we found $\Delta\text{Keff-nucl.}$ increases with the increase in the ^{238}U atomic density in six cases of hst001 [15]. Thus, we cannot assure the accuracy of these cross sections and their covariance matrices in the rapid energies when the atomic density of the ^{238}U increases.

5.5. Uncertainty on the Keff Produced by the Nuclear Data Uncertainties of the ^{16}O

Figure 8 shows the effect of cross sections uncertainties related to ^{16}O isotope on the effective multiplication factor (nucl. uncert. on Keff or $\Delta\text{Keff-nucl.}$) in different nuclear experiences. The uncertainties on the Keff produced by elastic, inelastic scattering, capture and fission cross sections and the effect of the correlation between them are represented by adjoint-weighted technique and by pcm ($1\text{pcm} = 10^{-5}$).

5.6. Interpretation and Conclusion on the Results of ^{16}O

The cross sections uncertainties have no effect on the effective multiplication factor (Keff) in all experiences, except the elastic scattering cross section uncertainty has the great contribution on the Keff uncertainties in the thermal experiences and in one rapid experience. Then, the elastic scattering cross section and its covariance matrix lack the adjustment especially in the thermal experiences.

5.7. Uncertainty on the Keff Produced by the Nuclear Data Uncertainties of the ^1H

Figure 9 shows the effect of cross sections uncertainties related to ^1H isotope on the effective multiplication factor (nucl. uncert. on Keff or $\Delta\text{Keff-nucl.}$) in different nuclear experiences. The uncertainties on the Keff produced by elastic, inelastic scattering, capture and fission cross sections and the effect of the correlation between them are represented by adjoint-weighted technique and by pcm ($1\text{pcm} = 10^{-5}$).

Figure 7. Uncertainties (pcm) produced by different cross sections of ^{238}U for different experiences

Figure 8. Uncertainties (pcm) produced by different cross sections of ^{16}O for different experiences

Figure 9. Uncertainties (pcm) produced by different cross sections of ^1H for different experiences

5.8. Interpretation and Conclusion on the Results of ^1H

– The cross sections uncertainties have no effect on the effective multiplication factor (K_{eff}) in all experiences, except the elastic scattering and the capture cross sections uncertainties have the great contribution on the K_{eff} uncertainties in the thermal experiences and in one rapid experience. Then, the elastic scattering and the capture cross sections and their covariance matrices lack the adjustment especially in the thermal experiences.

6. Conclusion

In this work we have analysed the sensitivities and

uncertainties on the effective multiplication factor (K_{eff}) produced by ENDF/B-VII.0 nuclear data; especially the elastic and inelastic scattering, capture and fission cross sections and their correlations in the ^1H , ^{16}O , ^{235}U and ^{238}U by the adjoint-weighted technique of the MCNP6 code. Firstly, we validated our perturbation technique in four experiences. After, a series of critical experiences have been studied by using the Monte Carlo code MCNP6 and the ERRORJ module of the last update NJOY99 to calculate the sensitivities vectors and to process the covariance matrices. In the end, the sensitivity vectors and covariance matrices are combined in order to obtain final uncertainties. As a conclusion:

– The four cross sections (elastic, inelastic, capture and

fission) of the ^{235}U and their covariance matrices Lack the adjustment especially in the rapid energies.

– The elastic cross section of the ^{16}O and its covariance matrice lack the adjustment especially in the thermal energies.

– The elastic and capture cross sections of the ^1H and their covariance matrices lack the adjustment especially in the thermal energies.

The adjustment of these cross sections and their covariance matrices is our aim in our future works.

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